



computer time for these (and other) factorizations. The method was implemented on the Cyber 205 by a team consisting of Herman J.J. te Riele, Walter M. Lioen and Dik T. Winter from the Department of Numerical Mathematics of the CWI. Advisory help was provided by J. Schlichting of Control Data.

The previous record for supercomputers was held by J.A. Davis and D.B. Holdridge from Sandia Labs (USA) who (in 1984) factorized the number  $(10^{71} - 1)/9$  (consisting of 71 1's) on a Cray X-MP24 of the Los Alamos Lab (USA) in 9.5 hours CPU-time, using a variant of the quadratic sieve method found by Davis ([1]). This Cray X-MP is about twice as fast as the Cyber 205 and has four million words of central memory (the Cyber 205 has one million words). In the heart of the quadratic sieve algorithm, the data to be handled are stored in non-contiguous memory locations. This is a handicap on the Cyber 205. All this illustrates the power of the Montgomery-variant of Pomerance's quadratic sieve.

It should be emphasized that larger difficult numbers have been factorized already by Robert Silverman, who did not use supercomputers, but VAX- and Sun-computers. His record is: a 81-digit composite number using a total of 1260 hours on 8 Sun 3/75 computers running in parallel. He also used the MPQS method.

Table 1: A few more details of our algorithm for the initiate:

	c72	c75
multiplier used:	none	5
factor base bound:	130000	160000
# primes in the factor base:	6071	7322
length of sieving interval:	$6(2^{16} - 1)$	$6(2^{16} - 1)$
# of completely factorized w's:	2672	3376
# of incompletely factorized w's:	24747	26062
# of large prime equalities in the incompletely factorized w's:	3401	3947
bound on the large primes allowed in incomplete w's:	$30 \times 130000$	$20 \times 160000$
Gauss elimination time (on a $6073 \times 6072$ , resp. $7323 \times 7323$ linear system):	21 sec.	37 sec.
# of dependencies found:	65	509

#### REFERENCES

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3. R.L. Rivest, A. Shamir, and L. Adleman. A method for obtaining digital signatures and public-key cryptosystems. *Communications of the ACM*, 21(2):120–126, February 1978.